

## PERCENTAGES

Concept:

By a certain percent, we mean that many hundredths.

Thus, x percent means x hundredths, written as x%.

To express x% as a fraction: We have,  $x\% = \frac{x}{100}$ .

$$\text{Thus, } 20\% = \frac{20}{100} = \frac{1}{5}$$

To express  $\frac{a}{b}$  as a percent: We have,  $\frac{a}{b} = \left(\frac{a}{b} \times 100\right)\%$ .

$$\text{Thus, } \frac{1}{4} = \left(\frac{1}{4} \times 100\right)\% = 25\%.$$

- 1.If A is R% more than B, then B is less than A by  $R / (100+R) * 100$
- 2.If A is R% less than B, then B is more than A by  $R / (100-R) * 100$
- 3.If the price of a commodity increases by R%, then reduction in consumption, not to increase the expenditure is :  $R/(100+R)*100$
- 4.If the price of a commodity decreases by R%, then the increase in consumption, not to decrease the expenditure is :  $R/(100-R)*100$

Results on Population:

Let the population of a town be P now and suppose it increases at the rate of R% per annum, then:

$$1. \text{ Population after } n \text{ years} = P \left(1 + \frac{R}{100}\right)^n$$

$$2. \text{ Population } n \text{ years ago} = \frac{P}{\left(1 + \frac{R}{100}\right)^n}$$

3. If a number is increased by x % and there after reduced by x %, then the number will be reduced by

$(x^2)/100$  percent.

4.If a number is reduced by x % and thereafter increased by x % then the number will be reduced

by  $\left(\frac{x^2}{100}\right)$  percent.

5. If in an examination, in which the minimum pass percentage is  $x\%$ , a candidate secures  $y$  marks and fails by  $z$  marks, then the total number

$$\frac{100 \times (y + z)}{x}$$

of marks in this examination will be

6. If in an examination  $x\%$  and  $y\%$  candidates respectively fail in two different subjects while  $z\%$  candidates fail in both the subjects, then the percentage of candidates who pass in both the subjects will

be  $[100 - (x + y - z)]\%$

TIPS:

1) If an object's price is increased or decreased by  $x\%$  and the other factor is decreased by  $y\%$  then the net effect is given by: Net Effect =  $[x + y + \frac{xy}{100}] \%$

2) If the net effect is nil, i.e. there is no loss or no gain, then the above formula becomes:  $y = \frac{100x}{100 + x}$

3) If the price of an article is successively increased by  $x\%$ ,  $y\%$  and  $z\%$  then single equivalent increase in the price will be  $[x + y + z + \frac{xy + yz + zx}{100} + \frac{xyz}{100^2}] \%$

4) If after spending  $p_1\%$  first, then  $p_2\%$  from the remaining and so on,  $B$  is the balance amount, then the total (original) amount is given by: Total amount =  $B \times 100 \times 100 \dots / (100 - p_1)(100 - p_2) \dots$  Population formula: 1) If the population increases by  $x\%$  during the first year, by  $y\%$  during the second year, by  $z\%$  during the third year, the population after three years will be:

$$P(1 + \frac{x}{100})(1 + \frac{y}{100})(1 + \frac{z}{100})$$