

Interest & Discount

IMPORTANT FORMULA AND EQUATIONS

Principal:

The money borrowed or lent out for a certain period is called the *principal* or the *sum*.

Interest:

Extra money paid for using other's money is called *interest*.

Simple Interest (S.I.):

If the interest on a sum borrowed for certain period is reckoned uniformly, then it is called *simple interest*.

Let Principal = P, Rate = R% per annum (p.a.) and Time = T years. Then

$$(i). \text{ Simple Interest} = \left(\frac{P \times R \times T}{100} \right)$$

$$(ii). P = \left(\frac{100 \times \text{S.I.}}{R \times T} \right); R = \left(\frac{100 \times \text{S.I.}}{P \times T} \right) \text{ and } T = \left(\frac{100 \times \text{S.I.}}{P \times R} \right).$$

Key notes on Simple interest

- Definition of Amount: If two equal principals are deposited for t_1 and t_2 years at $r_1\%$ and $r_2\%$ per annum such that the difference between their interests is D, then the principal can be obtained by $P = \frac{D \times 100}{r_1 t_1 - r_2 t_2}$.
- $SI = \frac{A \times R \times T}{100} + R \times T$
- $P = \frac{100 \times A}{100 + R \times T}$
- If a principal P becomes 'a' times of itself in T_1 years at $R_1\%$ rate per annum and 'b' times in T_2 years at $R_2\%$,
- then (i) $a - 1 / T_1 = b - 1 / T_2$
- (ii) $a - 1 / R_1 = b - 1 / R_2$
- If a person deposits Rs.x1 in a bank at $r_1\%$ per annum and Rs.x2 at $r_2\%$ per annum, then the interest for the whole sum is $[x_1 r_1 + x_2 r_2 / x_1 + x_2]\%$.

- If two equal principals are deposited for t_1 and t_2 years at $r_1\%$ and $r_2\%$ per annum such that the difference between their interests is D , then the principal can be obtained by $P = \text{Rs. } D \times 100 / r_1 t_1 - r_2 t_2$.

- If some Principal of money at simple interest amounts to Rs. A_1 in T_1 years and Rs. A_2 in T_2 years, then the sum and rate of interests are

$$\begin{aligned} \text{Principal} &= \frac{A_1 T_2 - A_2 T_1}{T_2 - T_1} \\ &= \frac{(A_2 - A_1) \times 100}{A_2 T_1 - A_1 T_2} \\ \text{Rate} & \end{aligned}$$

- A sum of money becomes n times itself in T years at simple interest, then the rate of interest is

$$\text{Rate} = \frac{100(n-1)}{T} \%$$

- If a sum of money becomes n times in T years at S.I then it will be m times of itself in years

$$\begin{aligned} \text{Required time} &= \frac{(m-1) \times T}{(n-1)} \text{ years} \\ & \frac{1}{x} \end{aligned}$$

- If S.I on a sum of money is $\frac{1}{x}$ th of the principal and the time T is equal to the rate percent R then

$$\text{Rate} = \text{Time} = \sqrt{100 \frac{1}{x}}$$

- A certain sum is at S.I at a certain rate for T years. And if it had been put at $R + 1\%$ higher rate, then it

$$= \frac{x \times 100}{T \times R_1}$$

would fetch Rs. x more Then the Principal

- The annual payment that will discharge a debt of Rs. P due in T years at the rate of interest $R\%$ per

$$= \frac{100P}{100T + \frac{RT(T-1)}{2}}$$

annum is Annual payment

- Let the rate of interest for first t_1 years is $r_1\%$ per annum, for the next t_2 years is $r_2\%$ per annum and for the period beyond that is $r_3\%$

Suppose all together the simple interest for t_3 years is Rs. I . Then

$$\begin{aligned} \text{Principal} &= \frac{100 \times I}{t_1 r_1 + t_2 r_2 + (t_3 - t_1 - t_2) r_3} \end{aligned}$$

- The simple interest on a certain sum of money at $r_1\%$ per annum for t_1 years is Rs. m . The interest on the same sum for t_2 years at $r_2\%$ per annum is n

$$\begin{aligned} \text{Then the sum} &= \frac{(m - n) \times 100}{r_1 t_1 - r_2 t_2} \end{aligned}$$